

Technology  
Science  
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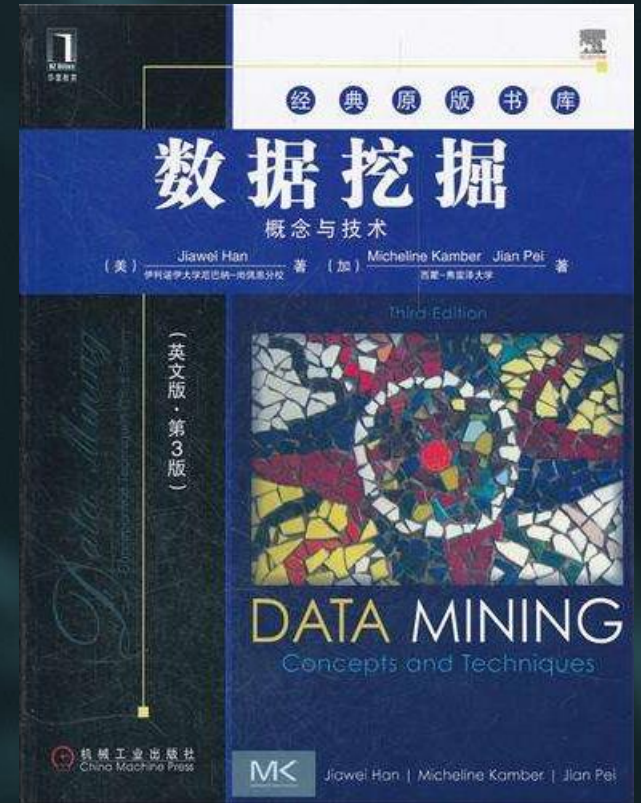
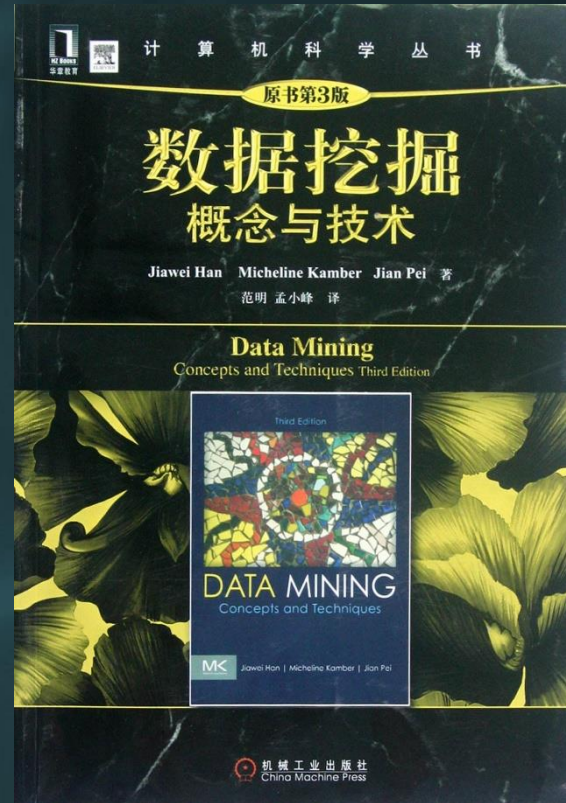
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# Chapter 8

## Classification: Basic Concepts



# Chapter 8: Classification

## 1. What is classification

a form of data analysis that extracts models describing data classes.

### Steps:

1. *Learning*: Training data are analyzed by a classification algorithm.
2. *Classification*: Test data are used to estimate the accuracy of the classification rules

## 2. Supervise learning (监督学习) and unsupervised learning (无监督学习)

### supervise learning:

- the learning of the classifier is “supervised” in that it is told to which class each training tuple belongs

### unsupervised learning (clustering) :

- the class label of each training tuple is not known, and the number or set of classes to be learned may not be known in advance



# Chapter 8

## 3. Decision Tree Induction

- Basic algorithm (a greedy algorithm)

### Conditions for stopping partitioning

- All samples for a given node belong to the same class
- There are no remaining attributes for further partitioning – majority voting is employed for classifying the leaf
- There are no samples left

Ref:

<https://blog.csdn.net/neilgy/article/details/82746270>

**Algorithm: Generate\_decision\_tree.** Generate a decision tree from the training tuples of data partition,  $D$ .

**Input:**

- Data partition,  $D$ , which is a set of training tuples and their associated class labels;
- *attribute\_list*, the set of candidate attributes;
- *Attribute\_selection\_method*, a procedure to determine the splitting criterion that “best” partitions the data tuples into individual classes. This criterion consists of a *splitting\_attribute* and, possibly, either a *split-point* or *splitting\_subset*.

**Output:** A decision tree.

**Method:**

- (1) create a node  $N$ ;
- (2) **if** tuples in  $D$  are all of the same class,  $C$ , **then**
- (3)     return  $N$  as a leaf node labeled with the class  $C$ ;
- (4) **if** *attribute\_list* is empty **then**
- (5)     return  $N$  as a leaf node labeled with the majority class in  $D$ ; // majority voting
- (6) apply *Attribute\_selection\_method*( $D$ , *attribute\_list*) to find the “best” *splitting\_criterion*;
- (7) label node  $N$  with *splitting\_criterion*;
- (8) **if** *splitting\_attribute* is discrete-valued **and**  
      multiway splits allowed **then** // not restricted to binary trees
- (9)     *attribute\_list*  $\leftarrow$  *attribute\_list* – *splitting\_attribute*; // remove *splitting\_attribute*
- (10) **for each** outcome  $j$  of *splitting\_criterion*  
      // partition the tuples and grow subtrees for each partition
- (11)     let  $D_j$  be the set of data tuples in  $D$  satisfying outcome  $j$ ; // a partition
- (12)     **if**  $D_j$  is empty **then**
- (13)         attach a leaf labeled with the majority class in  $D$  to node  $N$ ;
- (14)     **else** attach the node returned by *Generate\_decision\_tree*( $D_j$ , *attribute\_list*) to node  $N$ ;
- endfor**
- (15) return  $N$ ;

Basic algorithm for inducing a decision tree from training tuples.

# Chapter 8: Classification

## 4. Information Gain

$$\text{Gain}(A) = \text{Info}(D) - \text{Info}_A(D). \quad (8.3)$$

$$\text{Info}_A(D) = \sum_{j=1}^v \frac{|D_j|}{|D|} \times \text{Info}(D_j). \quad (8.2)$$

$$\text{Info}(D) = - \sum_{i=1}^m p_i \log_2(p_i), \quad (8.1)$$

# Chapter 8: Classification

## 5. Naïve Bayes Classifier

- ① Let  $D$  be a training set of tuples and their associated class labels, and each tuple is represented by an  $n$ -D attribute vector  $\mathbf{X} = (x_1, x_2, \dots, x_n)$
- ② Suppose there are  $m$  classes  $C_1, C_2, \dots, C_m$ .

Classification is to derive the maximum posteriori, i.e., the maximal  $P(C_i|\mathbf{X})$

This can be derived from Bayes' theorem

$$P(C_i|\mathbf{X}) = \frac{P(\mathbf{X}|C_i)P(C_i)}{P(\mathbf{X})}$$

- ③ Since  $P(\mathbf{X})$  is constant for all classes, only

$$P(C_i|\mathbf{X}) = P(\mathbf{X}|C_i)P(C_i)$$

needs to be maximized

# Chapter 8: Classification

## 6. Rule-based classification与decision tree

Ref:

[https://blog.csdn.net/weixin\\_42555080/article/details/91401493](https://blog.csdn.net/weixin_42555080/article/details/91401493)

## 7. Rule Generation

sequential covering algorithm

**Algorithm:** Sequential covering. Learn a set of IF-THEN rules for classification.

**Input:**

- $D$ , a data set of class-labeled tuples;
- $Att\_vals$ , the set of all attributes and their possible values.

**Output:** A set of IF-THEN rules.

**Method:**

```
(1)  $Rule\_set = \{\}$ ; // initial set of rules learned is empty
(2) for each class  $c$  do
(3)   repeat
(4)      $Rule = Learn\_One\_Rule(D, Att\_vals, c)$ ;
(5)     remove tuples covered by  $Rule$  from  $D$ ;
(6)      $Rule\_set = Rule\_set + Rule$ ; // add new rule to rule set
(7)   until terminating condition;
(8) endfor
(9) return  $Rule\_Set$ ;
```

Basic sequential covering algorithm.



# Chapter 8: Classification

## 8. Classification model evaluation

<i>Measure</i>	<i>Formula</i>
accuracy, recognition rate	$\frac{TP + TN}{P + N}$
error rate, misclassification rate	$\frac{FP + FN}{P + N}$
sensitivity, true positive rate, recall	$\frac{TP}{P}$
specificity, true negative rate	$\frac{TN}{N}$
precision	$\frac{TP}{TP + FP}$
$F$ , $F_1$ , $F$ -score, harmonic mean of precision and recall	$\frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$
$F_\beta$ , where $\beta$ is a non-negative real number	$\frac{(1 + \beta^2) \times \text{precision} \times \text{recall}}{\beta^2 \times \text{precision} + \text{recall}}$

Evaluation measures. Note that some measures are known by more than one name.  $TP$ ,  $TN$ ,  $FP$ ,  $P$ ,  $N$  refer to the number of true positive, true negative, false positive, positive, and negative samples, respectively (see text).



# Chapter 8: Classification

## 9. Bagging与Boosting

- Bagging: averaging the prediction over a collection of classifiers
- Boosting: weighted vote with a collection of classifiers

### 区别:

#### 1) 样本选择上:

**Bagging:** 训练集是在原始集中有放回选取的, 从原始集中选出的各轮训练集之间是独立的。

**Boosting:** 每一轮的训练集不变, 只是训练集中每个样例在分类器中的权重发生变化。而权值是根据上一轮的分类结果进行调整。

#### 2) 样例权重:

**Bagging:** 使用均匀取样, 每个样例的权重相等

**Boosting:** 根据错误率不断调整样例的权值, 错误率越大则权重越大。

#### 3) 预测函数:

**Bagging:** 所有预测函数的权重相等。

**Boosting:** 每个弱分类器都有相应的权重, 对于分类误差小的分类器会有更大的权重。

#### 4) 并行计算:

**Bagging:** 各个预测函数可以并行生成

**Boosting:** 各个预测函数只能顺序生成, 因为后一个模型参数需要前一轮模型的结果。

#### 5) bagging是减少variance, 而boosting是减少bias

# Chapter 8: Classification

## 10. Adaboost

## 11. Random forest

**Algorithm: AdaBoost.** A boosting algorithm—create an ensemble of classifiers. Each one gives a weighted vote.

**Input:**

- $D$ , a set of  $d$  class-labeled training tuples;
- $k$ , the number of rounds (one classifier is generated per round);
- a classification learning scheme.

**Output:** A composite model.

**Method:**

- (1) initialize the weight of each tuple in  $D$  to  $1/d$ ;
- (2) **for**  $i = 1$  to  $k$  **do** // for each round:
- (3)     sample  $D$  with replacement according to the tuple weights to obtain  $D_i$ ;
- (4)     use training set  $D_i$  to derive a model,  $M_i$ ;
- (5)     compute  $error(M_i)$ , the error rate of  $M_i$  (Eq. 8.34)
- (6)     **if**  $error(M_i) > 0.5$  **then**
- (7)         go back to step 3 and try again;
- (8)     **endif**
- (9)     **for** each tuple in  $D_i$  that was correctly classified **do**
- (10)         multiply the weight of the tuple by  $error(M_i)/(1 - error(M_i))$ ; // update weights
- (11)     normalize the weight of each tuple;
- (12) **endfor**

**To use the ensemble to classify tuple,  $X$ :**

- (1) initialize weight of each class to 0;
- (2) **for**  $i = 1$  to  $k$  **do** // for each classifier:
- (3)      $w_i = \log \frac{1 - error(M_i)}{error(M_i)}$ ; // weight of the classifier's vote
- (4)      $c = M_i(X)$ ; // get class prediction for  $X$  from  $M_i$
- (5)     add  $w_i$  to weight for class  $c$
- (6) **endfor**
- (7) return the class with the largest weight;

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AdaBoost, a boosting algorithm.

# Chapter 8: Classification

## 12. Imbalanced Data

- (1) oversampling,
- (2) undersampling,
- (3) threshold moving,
- (4) ensemble techniques





Next >> Chapter 9

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